

4.2

Irrational Numbers

Lesson 1

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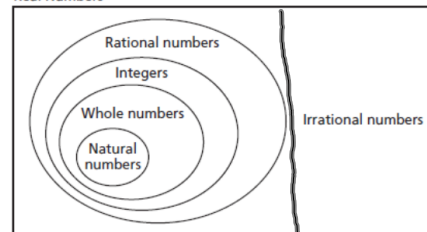
Connect

Number Sets

Up to Math 9 - you focused on Rational numbers. This year we are going to look at the other side - Irrational numbers.

Lets review the Number set Diagram.

Real Numbers



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Connect

Definitions:

Rational Number

Are numbers that have decimal representation that either terminate or repeat. They can also be put in the form $\frac{a}{b}$

Radicals that are square roots of perfect squares, cube roots of perfect cubes are also rational numbers.

Examples:

$$\sqrt{100} \quad \sqrt{0.25} \quad \sqrt{\frac{9}{64}} \quad \sqrt[5]{-32} \quad \sqrt[3]{8}$$

$$\frac{5}{6} \quad 0.8^2 \quad 0.5$$

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Radical. $\sqrt[n]{x}$ Radicals

n = is called the index

x = is called the radicand

Example: $\sqrt[5]{-32}$

Calculator: $5 \text{ [2nd] } \sqrt{x} \text{ [-] } 32 \text{ [=]} = \text{[-] } 2$

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Connect **Definitions:**

Irrational Number
 Are numbers that cannot be written in the form $\frac{a}{b}$, where a and b are integers, $n \neq 0$. The decimal representation of an irrational number neither terminates nor repeats.
 When an irrational number is written as a radical, the radical is the **exact value** of the irrational number.

Examples:
 $\sqrt{0.24}$ $\sqrt{2}$ $\sqrt{\frac{1}{3}}$ $\sqrt[4]{12}$ $\sqrt[3]{9}$

In the past we would have known that "Pi - π " would be a great example of an irrational number.

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Connect **Classifying Numbers**

Tell whether each number is rational or irrational. Explain how you know.

Rational *Irrational* *Rational*

$\frac{-3}{5}$ $\sqrt{14}$ $\sqrt[3]{\frac{8}{27}} = \frac{2}{3}$

$-\frac{6}{10}$ 3.741657387... 0. $\overline{6}$ Repeating

-0.6 terminates

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Practice **YOU TRY!**

Tell whether each number is rational or irrational. Explain how you know.

1.21 $\sqrt{\frac{49}{16}}$ $\sqrt[3]{-30}$

Rational $\frac{7}{4}$ -3.107232506

$1\frac{3}{4}$ *Rational* *Irrational*

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Express Decimals Into Fraction Form.

Ex 1: Non-Repeating Decimals

a) $0.48 = \frac{48}{100} = \frac{12}{25}$ b) $3.25 = 3\frac{25}{100} = \frac{325}{100} = \frac{13}{4}$

Ex 2: Repeating Decimals (Rule of 9's)

a) $0.\overline{8} = \frac{8}{9}$ b) $0.1231231... = \frac{123}{999}$

c) $3.21212121... = 3\frac{21}{99} = 3\frac{7}{33} = \frac{41}{33}$
 or $\frac{106}{33}$

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Ex 3: Special Case

$$a) 0.25555\dots = \frac{23}{90}$$

$$b) 0.1\bar{2} = \frac{11}{90}$$

$$c) 0.1\bar{23} = \frac{122}{990} = \frac{61}{495}$$

Practice

HOMEWORK!

Textbook Questions:

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